Gallium arsenide (GaAs) quantum photonic waveguide circuits

Jianwei Wang a, 1, Alberto Santamato a, 1, Pisu Jiang a, Damien Bonneau a, Erman Engin a, Joshua W. Silverstone a, Matthias Lermer b, Johannes Beetz b, Martin Kamp b, Sven Höfling a,c, Michael G. Tanner d, Chandra M. Natarajan e, Robert H. Hadfield d, Sander N. Dorenbos f, Val Zwoller f, Jeremy L. O’Brien a, Mark G. Thompson a, *

a Centre for Quantum Photonics, H H Wills Physics Laboratory and Department of Electrical and Electronic Engineering, University of Bristol, Merchant Venturers Building, Woodland Road, Bristol BS8 1UB, UK
b Technische Physik and Wilhelm Conrad Röntgen Research Center for Complex Material Systems, Universität Würzburg, Am Hubland, D-97074 Würzburg, Germany
c SUPA, School of Physics and Astronomy, University of St Andrews, St Andrews KY16 9SS, UK
d School of Engineering, University of Glasgow, Glasgow G12 8QQ, UK
e E. L. Ginzton Laboratory, Stanford University, Stanford 94305, USA
f Kavli Institute of Nanoscience, TU Delft, 2628CJ Delft, The Netherlands

A R T I C L E   I N F O
Article history:
Received 1 December 2013
Received in revised form 7 February 2014
Accepted 17 February 2014
Available online 4 March 2014

Keywords:
Quantum optics
Integrated quantum photonics
Quantum interference
Entanglement
GaAs waveguide
Pockels effect

A B S T R A C T
Integrated quantum photonics is a promising approach for future practical and large-scale quantum information processing technologies, with the prospect of on-chip generation, manipulation and measurement of complex quantum states of light. The gallium arsenide (GaAs) material system is a promising technology platform, and has already successfully demonstrated key components including waveguide integrated single-photon sources and integrated single-photon detectors. However, quantum circuits capable of manipulating quantum states of light have so far not been investigated in this material system. Here, we report GaAs photonic circuits for the manipulation of single-photon and two-photon states. Two-photon quantum interference with a visibility of 94.9 ± 1.3% was observed in GaAs directional couplers. Classical and quantum interference fringes with visibilities of 98.6 ± 1.3% and 84.4 ± 1.5% respectively were demonstrated in Mach–Zehnder interferometers exploiting the electro-optic Pockels effect. This work paves the way for a fully integrated quantum technology platform based on the GaAs material system.

© 2014 Elsevier B.V. All rights reserved.

1. Introduction

Quantum information science exploits fundamental quantum mechanical properties—superposition and entanglement—with the goal of dramatically enhancing communication security, computational efficiency and measurement precision [1–4]. Photons have been widely considered as an excellent physical implementation of quantum information and communication technologies due to their low dephasing, fast transmission and ease of manipulation [2, 5]. Bulk optical elements including single-photon sources, single-photon detectors and linear optical circuits have been successfully utilized to experimentally demonstrate quantum communication protocols, quantum metrology and small-scale quantum computation [6–9]. However, this bulk optics approach has severe limitations in terms of circuit stability, complexity and scalability.

The emergence of integrated quantum photonics (IQP) is revolutionising the field of photonic quantum technologies [10]. Utilizing well-developed integration technologies of classical photonics, IQP can shrink quantum experiments from a room-sized optical table onto a coin-sized semiconductor chip, and therefore greatly reduce the footprint of quantum devices and increase the complexity of quantum circuits [5, 10–24]. IQP inherently offers near-perfect mode overlap at an integrated beamsplitter for high-fidelity quantum interference [11, 15] and sub-wavelength stability of optical path lengths for high-visibility classical interference [13, 14], which are both essential to photonic quantum information processing. Recently, two-photon quantum interference with a visibility of > 99%, controlled-NOT quantum gate with a fidelity of 96%, and manipulations of entanglement have been demonstrated in the integrated photonic circuits, based on various platforms such as silica-on-silicon [11–15], laser direct writing silica [17–19], lithium niobate [20–22], silicon-on-insulator [23, 24], etc. Moreover, IQP would enable on-chip generation, manipulation and detection of quantum states of photons, ultimately required by practical and scalable quantum information processing technologies. Recently,
progress also has been made towards integrated single-photon sources and waveguide single-photon detectors. Periodically poled lithium niobate (PPLN) waveguides and silicon wire waveguides are examples of integrated waveguide sources for the generation of photon pairs via spontaneous parametric down conversion (SPDC) and spontaneous four-wave mixing (SFWM) respectively [25,26]. High-efficiency waveguides superconducting nanowire single-photon detectors (SNSPD) also have been successfully demonstrated in gallium arsenide (GaAs) waveguides and silicon wire waveguides [27,28].

Here, we report a low-loss GaAs/Al$_{0.3}$Ga$_{0.7}$As ridge waveguide platform for the manipulation of quantum states of light. GaAs is one of the most mature semiconductor materials widely used in classical integrated photonics. GaAs devices have been used for 100 GHz low-power modulation of optical signals [29] based on the strong electro-optical Pockels effect (driven by the large $\chi^2$ nonlinear coefficient of the GaAs material) and this linear index is linearly proportional to the applied electric field [30], and could provide a route to fast control and manipulation of photons for applications in quantum communication and quantum computation. Moreover, efficient on-chip single-photon sources have been developed based on semiconductor quantum dot embedded in the GaAs photonic crystal waveguides/cavities [31–37]. Spontaneous pair generation techniques have also been investigated using Bragg-reflection waveguides on GaAs platform to achieve the required phase-matching condition for spontaneous parametric down conversion [38–41]. GaAs waveguide integrated superconducting detectors have been demonstrated with efficiencies of 20% and short dead time of few ns [27], and photon number resolving capabilities [42]. Recently, photoluminescence from quantum dots has been coupled into the GaAs ridge waveguides and detected using the waveguide SNSPDs [43]. However, to-date no operations of photon’s quantum states have been reported in the GaAs waveguide photonic circuits. Based on our GaAs waveguide platform, we demonstrate the ability to control and manipulate two-photon quantum states, demonstrating two-photon quantum interference in directional couplers and utilizing Mach–Zehnder interferometers (MZIs) controlled electro-optically using the Pockels effect to realize quantum interference fringes. This work demonstrates important functionalities required for aGaAs integrated quantum technology platform, and presents essential quantum components for controlling quantum states, opening the way to the monolithic integration of quantum dot/SPDC single-photon sources, quantum photonic circuits and waveguide SNSPDs on a single GaAs wafer.

2. GaAs waveguides and experimental setup

Fig. 1(a) shows the cross section of a GaAs/Al$_{0.3}$Ga$_{0.7}$As ridge waveguide with a GaAs core and Al$_{0.3}$Ga$_{0.7}$As bottom/top claddings. The refractive indices of the GaAs core and Al$_{0.3}$Ga$_{0.7}$As claddings are 3.431 and 3.282 respectively, at the wavelength of 1550 nm. In order to meet the single-mode condition, the GaAs layer is etched down by 1.5 μm, forming the ridge waveguide with a width of 3.5 μm and a height of 3.9 μm. Fig. 1(a) also shows the simulated field distribution of the transverse electric (TE) fundamental mode using a finite difference mode (FDM) solver. Optical intensity distribution within the fabricated GaAs waveguide has been captured using an infrared CCD camera (Fig. 1(b)), which shows the single mode distribution. The Al$_{0.3}$Ga$_{0.7}$As/GaAs/Al$_{0.3}$Ga$_{0.7}$As layers which form the vertical waveguiding structure were alternately grown on top of a 100 nm-thin GaAs cap was also grown upon the top cladding to protect the Al$_{0.3}$Ga$_{0.7}$As layer against oxidation, and the GaAs substrate under the bottom cladding was doped to reduce the contact resistance. The waveguide circuits were defined by photolithography, using a 50 nm nickel film hard mask and lift-off process. The GaAs layer was inductively coupled plasma (ICP) etched, and the remaining nickel was removed before the chip was planarized by refilling the etched area with lift-off resist. A 200 nm gold film was sputtered after a second photolithography step, and gold contacts were patterned on top of MZIs arms by the lift-off process. Finally, the chip was cleaved for optical fiber coupling and mounted onto a chip holder for electrical connection. Fig. 1(c) shows the Scanning Electron Microscopy (SEM) images of the GaAs waveguides. Directional couplers and MZIs were both fabricated in this waveguide platform. The measured nominal propagation loss and coupling loss (between waveguides and lensed-fibers with a 2.5 ± 0.5 μm spot-diameter) using the Fabry–Perot method [44] was 1.6 dB/cm and 1.5 dB/facet respectively.

Photon pairs at 1550 nm wavelength were generated via type-II SPDC in a periodically poled potassium titanyl phosphate (PPLN) nonlinear crystal, pumped with a 50 mW continuous-wave laser at 775 nm wavelength (Fig. 2). Dichroic mirrors and a long-pass filter were used to separate the bright pump light from the photon pairs. Photon pairs with orthogonal polarization were separated by a polarization beamsplitter (PBS) and collected into two polarization-maintaining fibers (PMFs). Photons with horizontal polarization (corresponding to the TE mode of the waveguides) were coupled to the GaAs devices via two lensed single-mode fibers (lensed-SMFs), where the polarization orientation was corrected using two fiber polarization controllers for injection into the test devices. After the chip, photons were collected by two lensed-SMFs and detected using two single-photon detectors. Coincidences were recorded using a PicoHarp 300 Time Interval Analyzer (TIA). We used two different types of 1550 nm single-photon detectors: 1) two fiber-coupled superconducting single-photon detectors mounted in a closed cycle refrigerator with 1% and 4% efficiencies and ~1 kHz dark counts [45], used for the quantum interference experiment in the GaAs directional couplers.

**Fig. 1.** (a) Cross section of the GaAs/Al$_{0.3}$Ga$_{0.7}$As ridge waveguide and its simulated field distribution of the TE fundamental mode at 1550 nm wavelength, (b) measured intensity distribution of the TE fundamental mode at 1550 nm wavelength and (c) Scanning Electron Microscopy (SEM) images of the GaAs/Al$_{0.3}$Ga$_{0.7}$As waveguide.
and 2) two InGaAs/InP Avalanche photodiodes (APDs) from ID Quantique, one working in the free-running mode with a 10% efficiency and ~10 kHz dark counts and the other being triggered with a 20% efficiency and negligible dark counts, used for the investigation of single-photon superposition state and two-photon entanglement state in the GaAs MZIs. A rate of 2 x 10^6 Hz photon pairs from the SPDC source was observed and was used in the following experiments.

3. Quantum interference

Quantum information encoded on a photon can be realized using any of the different degrees of freedom of a photon, such as: path, time, polarization and orbital angular momentum [2,5,46]. In path encoding, the qubit is represented using the dual-rail encoding, where a photon in one of the two paths would be defined as |10⟩ and a photon in the other path would be defined as |01⟩. A single-qubit can therefore be represented as a superposition of these two states:

\[
|\Psi\rangle = \alpha|10\rangle + \beta|01\rangle
\]

where the photon is simultaneously present at |10⟩ and |01⟩ paths with respective probabilities of detection being |\alpha|^2 and |\beta|^2. The directional coupler (see Fig. 3(a)) is a typical form of integrated beamsplitter and performs an unitary operation of the single-qubit state [10]. Starting with an initial state of |10⟩ for instance, directional coupler rotates it into a superposition state of \(\sqrt{1-\epsilon}|10\rangle + i\sqrt{\epsilon}|01\rangle\), where \(\epsilon\) is the reflectivity or coupling ratio of the coupler (see details in Appendix A). When the coupling ratio \(\epsilon\) is equal to 0.5, the directional coupler performs a Hadamard-like operation and produces the state \(|\langle 10⟩ + i|01\rangle|/\sqrt{2}\). More interestingly, unique quantum interference occurs when two indistinguishable photons meet at a coupler with an \(\epsilon\) of 0.5 [47]. According to the interpretation of quantum mechanics, when two processes are indistinguishable, the probability of an event is equal to the complex square of their added probability amplitudes. Due to the \(\pi/2\) phase shift for any photon reflected from a beamsplitter, the probabilities of both photons being reflected or both transmitted cancel out; and therefore two photons injected on a coupler bunch together and produce a maximally path-entangled state as follows:

\[
|\langle 20⟩ + |02\rangle|/\sqrt{2}
\]
When two optical waveguides are placed closely together, light will couple back-and-forth between them via the evanescent field \[48\]. The coupling ratio \( e \) of the directional coupler depends on its coupling length and coupling strength. We designed and fabricated GaAs directional couplers with different coupling lengths and gaps for a control of the coupling ratio \( e \) (Fig. 3(a)). A directional coupler with near 0.5 coupling ratio was obtained when the gap was 2.5 \( \mu m \) and the coupling length was around 140 \( \mu m \) (Fig. 3(b)). The total length of the device was about 7 \( mm \) including four S-bends with a radius of 10 mm and the input/output waveguides (of separation 250 \( \mu m \)). Two input/output access-waveguides were distanced by 250 \( \mu m \) to allow access of the lensed-fibers for input/output coupling. At the 1550 nm wavelength, the fiber-to-fiber loss of the chip was measured to be \( 5-9 \) \( db \), with the internal devices losses (including the propagation loss and bends loss) estimated to be \( 3-8 \) \( db \). To characterize the device in the quantum regime, photon pairs from the SPDC source were launched to the GaAs directional coupler. A variable delay between the two injected photons was precisely controlled using a mechanical variable delay with a step of 20 \( \mu m \). After the chip, coincidences detection events were measured using two superconducting detectors and a TIA. Fig. 3(c) shows the Hong-Ou-Mandel (HOM) dip \[47\] with a visibility of 94.9 \( \pm 1.3 \) %, after a subtraction of accidental coincidences. At the center of HOM-dip, quantum interference results in the two photons coherently bunched together (as Formula (2)), and therefore minimal coincidences are recorded there. Observation of the high-visibility HOM-dip experimentally confirms two-photon quantum interference within the GaAs directional coupler. The triangular shape of the HOM-dip arises from the Fourier transform of the SPDC phase-matching sinc\(^2\) spectrum \[49\], which is narrower than the bandwidth of filters used in the SPDC source here. A triangular fit is used for estimating the visibility and shape of the HOM-dip. The shoulder-to-shoulder width of the HOM-dip is 440 \( \mu m \), indicating that the coherence time of each photon is 0.73 \( ps \) and coherent length in the waveguides is 64.1 \( \mu m \).

Furthermore, we measured the indistinguishability of photon pairs directly from the SPDC source using a fiber beamsplitter (\( e = 0.5 \)) connected with PMFs, resulting in maximum visibility of the HOM-dip of 98.7 \( \pm 0.6 \) %. Compared with the visibility for the GaAs coupler, a 3.8 % degradation of the visibility was observed and attributed to the strong Fresnel reflections at the waveguide facets due to the large refractive index difference. Since the coherence length of each photon is much shorter than the distance between the facets, we can ignore the Fabry–Perot self-interference of photons and only consider their back-and-forth reflections between waveguide facets. At each facet between GaAs waveguides and air, photons have a \( R \) probability of being reflected and a \( T \) probability of being transmitted. \( R \) and \( T \) are respectively calculated to be 30 % and 70 % using the Fresnel equation \( (n_{\text{GaAs}} - n_{\text{air}})/(n_{\text{GaAs}} + n_{\text{air}}))^2 \), where \( n_{\text{GaAs}} \) and \( n_{\text{air}} \) are refractive indices of GaAs and air. Firstly, consider the condition where the two photons undergo quantum interference and bunch at the output ports (i.e., center of the HOM-dip). Due to the reflections at the output facets photon \( A \) transmits with the \( T \) probability and photon \( B \) is reflected back with the \( R \) probability. Photon \( B \) can be reflected again at the input facets and leave out from another output port of the coupler with a phase-dependent probability. That is, round-trip reflections result in extra coincidences between photon \( A \) and photon \( B \) (see Appendix B), even in the case of perfect quantum interference. Note that time window for coincidences measurement was \( > 5 \) ns which was much longer than the first-order round-trip time delay of about 80 ps. Then, at the shoulder position of the HOM-dip corresponding to the distinguishable photons pairs input, we can use the same model to estimate the coincidences. Considering the loss within the chip, theoretical degradation of the visibility is estimated to be in the range of 0–4.4 %, which depends on the phase difference between two input-access-waveguides before the coupler. The experimental 3.8 % degradation of visibility is within this theoretical range and actually smaller than the worst degradation owning to a non-zero phase difference. The problem of reflection on facets could be resolved by applying anti-reflection coating on the waveguide facets. In future, for GaAs quantum circuits monolithically integrated with on-chip single-photon sources and detectors, reduction of the visibility due to the facet reflection could be ignored.

4. Manipulation of quantum states

Arbitrary unitary operations of quantum states, including preparation, manipulation and measurement of quantum states, are required to implement quantum communication and universal quantum computing. Generally, an arbitrary unitary operator on single-qubit can be decomposed of a set of rotations as \( U_{\text{arb}} = \exp \left( i\sigma_3 \right) \exp \left( i\sigma_2 \right) \exp \left( i\sigma_1 \right) \), which physically behaves as one Mach–Zehnder interferometer (MZI) and two additional phase shifters \[1\]. The MZI consisting of two beamsplitters and phase shifters is capable of controlling the relative phase and amplitude of the superposition state and entanglement state. When the single-photon state \( |10\rangle \) is launched into the MZI, the state transforms to

\[ |(1 - 2\epsilon) \cos(\theta/2) + i \sin(\theta/2) | (10) + 2\sqrt{\epsilon} (1 - \epsilon) \cos(\theta/2) | 01 \]  

where \( \theta \) is the relative phase between two arms and \( \epsilon \) is the coupling ratio of two directional couplers. An MZI with additional phase shifters enables arbitrary operations of the single-qubit states and therefore functionizes as the building-block for an experimental realization of arbitrary unitary \( N \times N \) operators \[50\] and also for the large-scale quantum information processors \[13\].

We fabricated GaAs MZIs with two electro-optical phase shifters which enable an independent control of the phases of two arms (Fig. 4(a)). When an electric field \( E \) is applied along the (100) direction (vertically), the refractive index of the TE mode linearly responds to the electric field as \( \Delta n = n_{\text{GaAs}} r_2 E/2 \), where \( r_2 \approx 1.4 \times 10^{-12} \) m/V is the electro-optical coefficient of the GaAs material \[51\]. The length of the phase shifters was 10 cm and voltage required to induce a \( \pi \) phase shift (\( V_\pi \)) was measured to be 13 V. The two couplers within the MZI were designed identically with a gap of 3.0 \( \mu m \) and a coupling length of 255 \( \mu m \). The total length of the MZI chip was about 1.7 cm (Fig. 4(b)) and fiber-to-fiber loss of the chip was measured to be \( 10.3 \) \( db \). Classical characterization of the device was performed using coherent bright-light from a tunable laser diode, and also single-photons from the SPDC source were individually routed to the MZI devices for a characterization of classical interference. Two power-meters and two APDs were respectively used to detect the bright-light intensities and single-photon counts at two output ports of the MZI. By linearly scanning the applied voltages on two arms, we observed the classical interference fringes for both bright-light and single-photons which exhibited the same periodicity. Fig. 4(c) shows the normalized classical interference fringes as a function of relative phase shift for the coherent bright-light input. One can see that the classical interference fringes for two outputs are unbalanced and have different maximum visibilities of 98.6 \( \pm 1.3 \) % and 79.9 \( \pm 4.9 \) %. The unbalance of the interference fringes arises from the non-0.5 coupling ratios of two directional couplers. The coupling ratio of individual coupler was measured to be approximately 0.3 (Fig. 3(b)). According to Formula (3), single-photon counts or bright-light intensities from two outputs respectively vary as \( |\sin(\theta/2) + \cos^2(\theta/2)(1 - 2\epsilon) + 4\epsilon(1 - \epsilon) \cos(\theta/2)|^2 \), and we...
Double frequency was observed and shown in Fig. 4(d), indicating fringes above, two-photon quantum interference fringe with a time-indistinguishability. Compared with the classical interference of them arrive at the MZI simultaneously and therefore guarantee the delay between the two photons was carefully controlled to make sinusoidal outputs as sin2(θ/2) and cos2(θ/2) and therefore result in well-balanced and higher-visibility classical interference fringes. Note that we actually had MZIs with ε close to 0.5; however, they unfortunately suffered high loss which made it unfeasible to characterize these devices in the two-photon quantum interference experiments. Then we used the MZI with ε~0.3 for the investigation of quantum interference within these devices.

Generally, when two indistinguishable photons are separately launched into two input ports of the MZI, quantum interference at the first coupler with an arbitrary coupling ratio creates the two-photon state:

$$\sqrt{2}\epsilon(1-\epsilon)[|20\rangle + |02\rangle] + (1-2\epsilon)|11\rangle$$  \hspace{1cm} (4)

(For details see Appendix A). Note that when ε is equals to 0.5 the two photons are maximally path-entangled, as in Formula (2). The phase shifters within the MZI then perform a z-axis rotation on the state, and the second coupler acts to further transform the state to:

$$\sqrt{2}\epsilon(1-\epsilon)[-\epsilon e^{-i2\theta} + (1-2\epsilon)e^{-i\theta} + (1-\epsilon)]|20\rangle$$

$$+ \sqrt{2}\epsilon(1-\epsilon)[(1-\epsilon)e^{-i2\theta} + (1-2\epsilon)e^{-i\theta} - \epsilon]|02\rangle$$

$$+ [-2\epsilon(1-\epsilon)e^{-i2\theta} + (1-2\epsilon)^2e^{-i\theta} - 2\epsilon(1-\epsilon)]|11\rangle$$  \hspace{1cm} (5)

To characterize the performance of the device in the two-photon quantum regime, we routed photons pairs from the SPDC source to the MZI and recorded coincidences (corresponding to the |11\rangle term in Formula (5)) using two APDs and the TIA. The time delay between the two photons was carefully controlled to make them arrive at the MZI simultaneously and therefore guarantee the time-indistinguishability. Compared with the classical interference fringes above, two-photon quantum interference fringe with a double frequency was observed and shown in Fig. 4(d), indicating a manipulation of the two-photon entanglement state. The maximum visibility is measured to be 84.4±1.5%, which is greater than the requirement of beating the standard quantum limit [52].

The visibility of quantum interference fringe is non-uniform owing to the unbalance of the directional couplers [53]. The coexistence of the $e^{-i\theta}$ and $e^{-i2\theta}$ terms in Formula (5) leads to the non-uniformity of the interference fringe when ε is away 0.5. The solid line in Fig. 4(d) depicts the theoretical two-photon interference fringe when ε is chosen as 0.3. The shape and periodicity between the theoretical fringe and experimental result agree well, whereas deviation at the bottom likely arises from the polarization distinguishability induced in SMFs before the chip. In addition, two photons may carry a small transverse magnetic (TM) component, which does not respond to the applied electric field, and behave as the coincidences background independent of the phase shift. If a coupling ratio of 0.5 is used, Formula (5) can be simply reduced to $sin(\theta)|20\rangle - |02\rangle)/\sqrt{2} + cos(\theta)|11\rangle$, resulting in pure double-frequency quantum interference fringe [13,14]. Through further device optimization, controlling coupling ratios and polarization of photons, quantum interference with uniform distribution and higher visibility would be achievable.

5. Conclusion

To summarize, we have developed a GaAs ridge waveguide technology platform for integrated quantum photonic circuits. Directional couplers and MZIs were fabricated and their suitability for quantum interference experiments assessed. We demonstrated two-photon quantum interference with a high-visibility using the directional couplers and implemented the manipulation of two-photon state using MZIs. This study demonstrates the feasibility of quantum waveguide circuits in GaAs, opening the way to a fully integrated quantum technology platform where single photon sources, detectors and waveguide circuits could be combined in a single GaAs chip. This approach is promising for a large-scale and
practical integrated platform for on-chip quantum information processing.

Acknowledgments

This work was supported by the European FP7 project Quantum Integrated Photonics (QUANTIP), the Engineering and Physical Sciences Research Council (EPSRC), the European Research Council (ERC) and the Bristol Centre for Nanoscience and Quantum Information (NSQ). A.S. is supported by a DSTL National PhD scheme studentship. R.H.H. acknowledges a Royal Society University Research Fellowship. V.Z. acknowledges support from the Dutch Foundation for Fundamental Research on Matter. J.L.O’B. acknowledges a Royal Society Wolfson Merit Award.

Appendix A

Unitary operator of the directional coupler with an arbitrary coupling ratio or reflectivity $\varepsilon$ is shown as:

$$
\begin{bmatrix}
\sqrt{1-\varepsilon} & i\sqrt{\varepsilon} \\
\sqrt{\varepsilon} & \sqrt{1-\varepsilon}
\end{bmatrix}
$$

(A1)

We use the quantum mechanical representation to describe the unitary transformations applied by the directional coupler and Mach–Zehnder interferometer (MZI) as following. $\hat{a}_i$ and $\hat{a}_f$ are the annihilation and creation operators, respectively, and $i$ is the port number in Fig. A1.

When one-photon state $|10\rangle=\hat{a}_i^+|00\rangle$ is launched into the directional coupler, the state is rotated as:

$$
|10\rangle \xrightarrow{DC} (\sqrt{1-\varepsilon}\hat{a}_i^+ + i\sqrt{\varepsilon}\hat{a}_f^+) |00\rangle = \sqrt{1-\varepsilon} |10\rangle + i\sqrt{\varepsilon} |01\rangle
$$

(A2)

When one-photon state $|10\rangle=\hat{a}_f^+|00\rangle$ is launched into the MZI, the state is rotated as:

$$
|10\rangle \xrightarrow{MZI} (\sqrt{1-\varepsilon}\hat{a}_i^+ + i\sqrt{\varepsilon}\hat{a}_f^+) |00\rangle \xrightarrow{Phase shifter} (\sqrt{1-\varepsilon}\hat{a}_i^+ + e^{-i\phi}i\sqrt{\varepsilon}\hat{a}_f^+) |00\rangle
$$

$$
\xrightarrow{DC} (\sqrt{1-\varepsilon}\hat{a}_i^+ + i\sqrt{\varepsilon}\hat{a}_f^+ + e^{-i\phi}e^{i\theta}(\sqrt{1-\varepsilon}\hat{a}_i^+ + \sqrt{1-\varepsilon}\hat{a}_f^+)) |00\rangle
$$

$$
|1-2\varepsilon|\cos(\theta/2) + is\sin(\theta/2)|10\rangle + i2\sqrt{\varepsilon(1-\varepsilon)} \cos(\theta/2)|01\rangle
$$

(A3)

When two-photon state $|11\rangle=\hat{a}_i^+\hat{a}_f^+|00\rangle$ is launched into the directional coupler, the state is rotated as:

$$
|11\rangle \xrightarrow{DC} (\sqrt{1-\varepsilon}\hat{a}_i^+ + i\sqrt{\varepsilon}\hat{a}_f^+) (\sqrt{1-\varepsilon}\hat{a}_i^+ + \sqrt{1-\varepsilon}\hat{a}_f^+) |00\rangle
$$

$$
= (\sqrt{1-\varepsilon})^2 (\hat{a}_i^+\hat{a}_i^+ + \hat{a}_f^+\hat{a}_f^+) + (1-2\varepsilon)\hat{a}_i^+\hat{a}_f^+ + (1-2\varepsilon)\hat{a}_f^+\hat{a}_i^+) |00\rangle
$$

$$
= 2\varepsilon(1-\varepsilon) (\hat{a}_i^+|20\rangle + |02\rangle) + (1-2\varepsilon) |11\rangle
$$

(A4)

When two-photon state $|11\rangle=\hat{a}_i^+\hat{a}_f^+|00\rangle$ is launched into the MZI, the state is rotated as:

$$
|11\rangle \xrightarrow{MZI} (\sqrt{1-\varepsilon}\hat{a}_i^+ + i\sqrt{\varepsilon}\hat{a}_f^+) (\sqrt{1-\varepsilon}\hat{a}_i^+ + \sqrt{1-\varepsilon}\hat{a}_f^+ + e^{-i\phi}e^{i\theta}(\sqrt{1-\varepsilon}\hat{a}_i^+ + \sqrt{1-\varepsilon}\hat{a}_f^+)) |00\rangle
$$

$$
\xrightarrow{Phase shifter} (\hat{a}_i^+\hat{a}_i^+ + e^{-i\phi}\hat{a}_f^+\hat{a}_f^+ + (1-2\varepsilon) e^{-i\phi}\hat{a}_i^+\hat{a}_f^+ + (1-2\varepsilon)e^{-i\phi}\hat{a}_f^+\hat{a}_i^+) |00\rangle
$$

$$
\xrightarrow{DC} (2\varepsilon(1-\varepsilon)\hat{a}_i^+|20\rangle + (1-2\varepsilon) e^{-i\phi}(1-\varepsilon) e^{-i\phi}|02\rangle + (1-2\varepsilon)e^{-i\phi}\hat{a}_f^+|02\rangle + (1-2\varepsilon) e^{-i\phi} e^{-i\phi}\hat{a}_f^+|11\rangle + 1|20\rangle + 1|02\rangle + (1-2\varepsilon) e^{-i\phi} e^{-i\phi}|11\rangle
$$

(A5)

Appendix B

Coherence length of each photon is much shorter than the chip length and therefore we could ignore the Fabry–Perot self-interference and only consider the forth-and-back reflections for photons. At each waveguide facet, photons have an $R$ probability of being reflected and a $T$ probability of being transmitted. $R$ and $T$ are estimated using the Fresnel equation.

Fig. B1(a) shows the forth-and-back reflection at the dip position of the HOM-dip, where two photons should be coherently bunched in the ideal case. For example, photon $A$ (red) and photon $B$ (blue) have a 50% probability of being bunched at port 3. Due to the facet reflection, photon $A$ have the $T$ probability of transmitting and photon $B$ has the $R$ probability of being reflected. Then photon $B$ is reflected again at the input facets, and consequently there is a chance that photon $B$ will leave out from port 4 of the coupler and coincide with photon $A$. Note that photon $B$ passes the directional coupler ($\varepsilon=0.5$) twice and a “MZI”-like interference will occur. Any variation of waveguides width/length and angle-cleave of the input access-waveguides will induce phase difference $\Delta\phi$ between two input waveguides before the coupler. Therefore, the probability of extra coincidences depends on the phase difference $\Delta\phi$. When only considering the first-order round-trip of reflections, coincidences at the dip position will be:

$$
NR^2 T^4 \eta_1^2 \eta_2^2 \cos^2(\Delta\phi/2) \eta_{a1} \eta_{a2}
$$

(B1)

where $N$ is the rate of photon pairs of the SPDC source, and $\eta_c$ is the coupling loss and $\eta$ is the loss within the chip (including the propagation loss and bending loss), and $\eta_{a1}$ and $\eta_{a2}$ are efficiencies of two detectors.

Similarly, we can analysis the shoulder of the HOM-dip, where two distinguishable photons are injected and four different processes occur: both reflected, both transmitted, and one reflected and one transmitted. Fig. B1(b) and (c) shows the zero-order and

![Fig. A1. Schematic diagrams of the (a) directional coupler and (b) Mach–Zehnder interferometer.](image-url)
first-order round-trips when photon A and B are initially anti-bunched. Coincidences at the shoulder position of the HOM-dip will be:

$$N|T|^4|N|^4/2 + \sin^2(\Delta \phi/2)|R|^4|N|^4/2 + \cos^2(\Delta \phi/2)|R|^4|N|^4/2|\eta_1\eta_2$$

(B2)

According to Formulas (B1) and (B2), the theoretical visibility is estimated to be in the range of 95.6–100%, corresponding to a degradation of the visibility in the range of 0–4.4%, which depends on the phase difference $\Delta \phi$ between two input access-waveguides before the coupler. The worst degradation of the visibility is 4.4% when $\Delta \phi$ is chosen to be zero.

References